

Probability Smoothing for NLP
A case study for functional programming
and little languages

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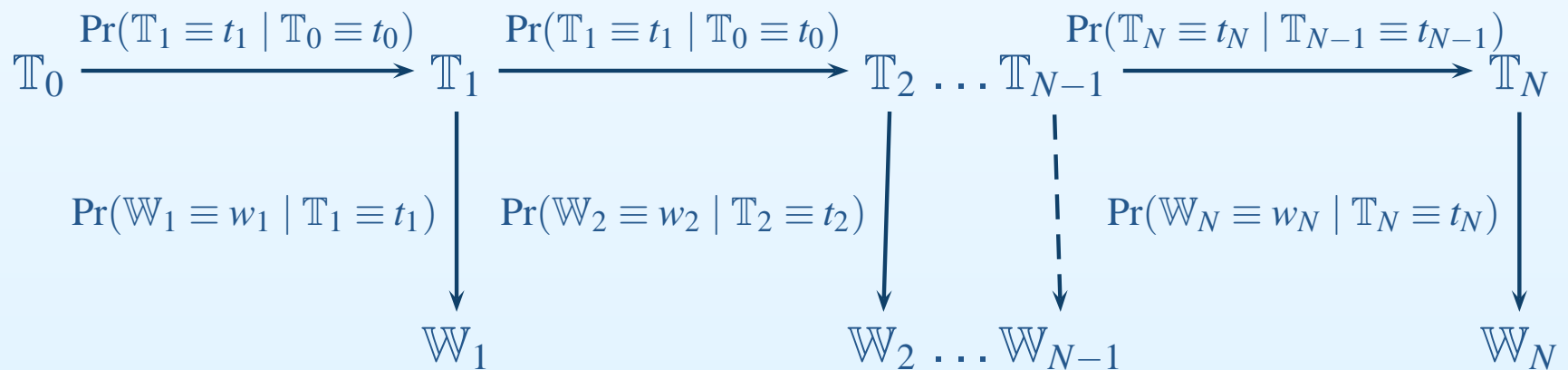
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Outline of the talk

- What is the domain?
 - Statistical natural-language processing (NLP)
 - More specifically: part-of-speech (POS) tagging
 - More specifically: ...using hidden Markov models (HMMs)
- What is the problem?
 - Keeping models and algorithms separate, modular
 - Specifying different smoothed models quickly and easily
- The solution
 - A little language
- But what is the problem, really?
 - Achieving high performance, despite modularity
- The revised solution
 - Partial evaluation for loop-invariant code motion

What is the domain?

- Statistical NLP
 - But don't worry if you can't follow the stats
- POS (and other) tagging
 - Given a sequence of words, w_1^N , figure out a sequence of tags, t_1^N , one for each word
- (first-order) HMMs for tagging
 - The “noisy channel model”



What is the problem?

- Keeping models and algorithms separate, modular
 - Should be trivial, but noone seems to do it; why?
 - Will be talked about more later
- Specifying different smoothed models quickly and easily
 - Where do we get those probabilities from?
 - from a model
 - What is a model?
 - a function estimating the true probabilities of events
 - The model is “trained” on some example data
 - i.e., given the data, choose from a family of functions
 - Many different ways to extrapolate from the training data
 - which family do we choose from?

What is a model?

- The MLE (maximum likelihood estimate) model, aka unsmoothed model

$$p_{MLE}(x | y) \models \Pr(x | y)$$

$$p_{MLE}(x | y) = \frac{c_{XY}(x, y)}{c_Y(y)}$$

where

$c_{XY}(x, y)$ = the count of times an $(x \wedge y)$ joint event was observed

$c_Y(y)$ = the count of times a y event was observed

$$c_Y(y) = \sum_{x \in X} c_{XY}(x, y)$$

- The MLE model maximizes the likelihood of the training data, but it underestimates the likelihood of unseen events; i.e.,

$$c_X(x) = 0 \implies p_{MLE}(x | y) = 0$$

What is a model?

- Add-1 smoothing (aka, Laplace's law)

$$p_{+1}(x | y) \models \Pr(x | y)$$

$$p_{+1}(x | y) = \frac{c_{XY}(x, y) + 1}{c_Y(y) + |X|}$$

- Nice: guarantees no zero probabilities for novel events
- Bug: for large domains of possible events it gives too much probability to the novel events

What is a model?

- Add- λ smoothing (aka, Lidstone's law, add- δ smoothing, additive smoothing)

$$p_{+\lambda}(x | y) \models \Pr(x | y)$$

$$p_{+\lambda}(x | y) = \frac{c_{XY}(x, y) + \lambda}{c_Y(y) + \lambda * |X|}$$

- Better, but it requires estimating the parameter λ , and it still doesn't solve the problem in principle

What is a model?

- Chen–Goodman smoothing (aka, one-count smoothing)

$$p_{CG}(x | y) \models \Pr(x | y)$$

$$p_{CG}(x | y) = \frac{c_{XY}(x, y) + s_{XY}(y) * p'(x | y)}{c_Y(y) + s_{XY}(y)}$$

where

$s_{XY}(y)$ = the count of $x \in X$ such that $c_{XY}(x, y) = 1$

$p'(x | y) \models \Pr(x | y')$ where $y' \subset y$

- And others: linear interpolation, Good–Turing, Katz backoff, Witten–Bell, Kneser–Ney, Jelinek–Mercer, Church–Gale, Moore–Quick, and numerous variants

The solution, pt. I

- What is a model?
 - A **function** estimating the true probabilities of events
- A statistical take on the Curry–Howard isomorphism: Probabilities as types; distributions as values
 - $p(x | y) \models \text{Pr}(x | y) \implies p : X \rightarrow Y \rightarrow \mathbb{P}$
 - $c_X(x) \implies c_X : X \rightarrow \mathbb{C}$
- The types \mathbb{P} and \mathbb{C} are related by a kind of module structure We'll gloss over the details, but suffice it to say that
 - $\exists(+): \mathbb{C} \rightarrow \mathbb{C} \rightarrow \mathbb{C}$
 - $\exists(*): \mathbb{C} \rightarrow \mathbb{P} \rightarrow \mathbb{C}$ (or $\mathbb{P} \rightarrow \mathbb{C} \rightarrow \mathbb{C}$)
 - $\exists(\div): \mathbb{C} \rightarrow \mathbb{C} \rightarrow \mathbb{P}$
- With these, we can define a combinator library

The solution, pt. I

unsmoothed : $(X \rightarrow Y \rightarrow \mathbb{C}) \rightarrow (Y \rightarrow \mathbb{C}) \rightarrow (X \rightarrow Y \rightarrow \mathbb{P})$

$$\text{unsmoothed}(c_{XY}, c_Y) = \lambda x y. c_{XY}(x, y) \div c_Y(y)$$

addOne : $(X \rightarrow Y \rightarrow \mathbb{C}) \rightarrow (Y \rightarrow \mathbb{C}) \rightarrow \mathbb{C} \rightarrow (X \rightarrow Y \rightarrow \mathbb{P})$

$$\text{addOne}(c_{XY}, c_Y, |X|) = \lambda x y. (c_{XY}(x, y) + 1) \div (c_Y(y) + |X|)$$

$$\text{addLambda}(c_{XY}, c_Y, \delta, |X|) = \lambda x y. (c_{XY}(x, y) + \delta) \div (c_Y(y) + \delta * |X|)$$

$$\text{chenGoodman}(c_{XY}, c_Y, s_{XY}, p') = \lambda x y. (c_{XY}(x, y) + s_{XY}(y) * p'(x | y)) \div (c_Y(y) + s_{XY}(y))$$

- Combinators like these make it easy to specify complex smoothing methods, as well as being clear and explicit about it

But what is the problem really?

- Keeping models and algorithms separate, modular
 - Using HOFs makes this easy
- ... While achieving high performance
 - These probability distributions will be evaluated inside triply nested loops: $\forall i. \forall y_i. \forall x_i. p(x_i | y_i)$ (or worse)
- Standard optimizations from imperative programming aren't available; e.g., loop invariant code motion
 - ... Or are they?

Loop invariant code motion

- Lifting invariant code **can** improve asymptotic performance
 - $O(m * (n + o)) \implies O(n + m * o)$
- So-called “constant” factors should not be ignored, because parameters are not constant in practice
 - The first-order Forward algorithm is $O(T^2 * N)$, not $O(N)$
- Idea: use partial evaluation to perform LICM dynamically
 - We know the order of the loops: y is outer, x is inner
 - $p(x | y) \models \text{Pr}(x | y) \implies p: Y \rightarrow X \rightarrow \mathbb{P}$
 - Now we can take the partial *application*, $p(y)$, and perform partial *evaluation*
 - $p(y): X \rightarrow \mathbb{P} \implies p_y(x) \models \text{Pr}(x | y)$

LICM example

```
chenGoodman cyx cy syx pyx y = let
```

```
  !cyx_y = cyx y
```

```
  !pyx_y = pyx y
```

```
  !syx_y = syx y
```

```
  !z      = cy y + syx_y
```

```
in  $\lambda$  x  $\rightarrow$  (cyx_y x + syx_y * pyx_y x) / z
```

Dynamic LICM

- Original benchmark: gives 10% total-runtime reduction
 - Includes extraneous things like I/O (for an I/O-bound program)
 - Actual improvement is superlinear (because of the asymptotic role of T)
- All the details are hidden away in the library
 - that 10% improvement required **no** client code changes
- Caveat lector
 - More recent benchmarks are less impressive
 - only 3%, excluding all extraneous factors
 - no observed non-linear behavior
 - This is due to algorithmic optimizations since then
 - but that's an orthogonal concern

Conclusions

- Allows us to perform LICM *at runtime*
 - With a JIT, could fuse the model and the algorithm
 - to remove indirection overhead
 - Or we can do LICM and fusion at compile time via `{-# INLINE #-}` pragma
- Retains separation of concerns
 - Don't pollute the algorithm with modeling concerns
 - Don't base the algorithm around a particular model
- Keeps code legible
 - Say what you mean, not how to optimize it
 - All the details are hidden away in the library

~fin.